

Representation of Real Numbers  
Problem A

If  $p=1$ ,  $e_{\min} = -1$  and  $e_{\max} = 1$

- 1) List the possible *positive* floating point numbers.
- 2) Can the following numbers or expressions be represented (exactly)? If not, why not?  
  
50  
500  
55  
 $0.05 * .5$
- 3) If  $x = 14.5$ , what is the  
  
roundoff error  
  
relative error

Representation of Real Numbers  
Problem A - Answers

If  $p=1$ ,  $e_{\min} = -1$  and  $e_{\max} = 1$

- 1) List the possible *positive* floating point numbers.  
  
0.1, 0.2, ...0.9, 1, 2, 3, ...9, 10, 20, 30, ...90
- 2) Can the following numbers or expressions be represented (exactly)? If not, why not?  
  
50 - yes  
500 - no neither  $50 \times 10^1$  or  $5 \times 10^2$  are allowed  
55 - no, this requires a two-digit mantissa  
 $0.05 * .5$  - 0.0025 requires a two-digit mantissa and it's less than 0.1
- 3) If  $x = 14.5$ , what is the  
  
roundoff error             $|14.5 - 10| = 4.5$   
relative error             $4.5 / 14.5 = 0.31$

## Representation of Real Numbers Problem B

- 1) Assume we change  $p$  to 2 in Problem A so that we can have 2-digit mantissas. Now, for the range  $[10..100)$ , we can support every whole number, i.e., 10, 11, 12,... 98, 99.

If  $x = 14.5$ , what is the

roundoff error

relative error

- 2) With  $p=2$ , now set  $e_{min} = -2$  and  $e_{max} = 2$ .

What is the largest floating point number that can be represented?

## Representation of Real Numbers Problem B - Answers

- 1) Assume we change  $p$  to 2 in Problem A so that we can have 2-digit mantissas. Now, for the range  $[10..100)$ , we can support every whole number, i.e., 10, 11, 12,... 98, 99.

If  $x = 14.5$ , what is the

roundoff error       $|14.5 - 14| = 0.5$

relative error       $0.5 / 14.5 = 0.034$

- 2) With  $p=2$ , now set  $e_{min} = -2$  and  $e_{max} = 2$ .

What is the largest floating point number that can be represented?

$9.9 \times 10^2 = 990$  note: the mantissa is in the range  $[1.0 ..10.0)$